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ACHIEVERS In Focus Vol.8 Issue-11

ACHIEVERS In Focus

$$=1 \div \left[1+1 \div \frac{3}{3}\right] = 1 \div \left[1+\frac{3}{5}\right] = 1 \div \frac{3}{5} = \frac{3}{8}$$
27. (d) $2\sqrt[3]{40} = 4\sqrt[3]{5}$, $4\sqrt[3]{320} = 16\sqrt[3]{5}$,
 $3\sqrt[3]{625} = 15\sqrt[3]{5}$
 $\therefore 2\sqrt[3]{40} - 4\sqrt[3]{320} + 3\sqrt[3]{625} - 3\sqrt[3]{5}$
 $= 4\sqrt[3]{5} - 16\sqrt[3]{5} + 15\sqrt[3]{5} - 3\sqrt[3]{5} = 0$
28. (d) $123 - 99 = 24$ $183 - 123 = 60$
 $183 - 99 = 84$
HCF of 24, 60, 84 $\frac{12|24, 60, 84}{2, 5, 7}$

 $=1\div \left| 1+1\div \left\{ 1+1\div \frac{3}{2} \right\} \right|$

 $=1\div\left[1+1\div\left\{1+\frac{2}{3}\right\}\right]$

29. (b)
$$\frac{a}{b} = \frac{b}{c}$$

 $\Rightarrow b^2 = ac \Rightarrow b^4 = a^2c^2$
 $\therefore \frac{a^4}{b^4} = \frac{a^4}{a^2c^2} = \frac{a^2}{c^2}$
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30. (a) Here, rule of alligation is applied for number of legs per head.

Average number of legs per head $=\frac{290}{100}=\frac{29}{10}$



 \therefore Lions : Parrots = 9 : 11

Number of parrots
$$=\frac{11}{20} \times 100 = 55$$

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31. (a) $4200 = \frac{29400 \times 6 \times R}{100}$

$$\Rightarrow R = \frac{4200}{294 \times 6} = \frac{50}{21} = 2\frac{8}{21}\%$$

32. (a) Let the M.P. be Rs 100. Then,
$$C.P. = Rs 64$$
.

Gain% =
$$\left(\frac{24}{64} \times 100\right)$$
% = $\frac{75}{2}$ % = 37.5%

33. (b) According to question, (A's 1 day's work) : (B's 1 day's work) = 2:1Now, (A + B)'s 1 day's work $\frac{1}{12}$ ∴ B's 1 day's work **ACHIEVERS** In Focus $= \frac{1}{12} \times \frac{1}{3} = \frac{1}{36}$ $\therefore \text{ B can finish the whole work in 36 days.}$ Speed at upstream = $\frac{36}{6}$ = 6km/hr. 34. (d) Speed at downstream = $\frac{48}{6}$ = 8 km/hr \therefore Speed of the current = $\frac{8-6}{2}$ = 1 km/hr. 35. (c) Let the average after 19th inning be x. Then, average after 18th inning = (x - 4). 19x - 18(x - 4) = 98 \Rightarrow x + 72 = 98 \Rightarrow x = 26 \therefore Average after 19th inning = 26 36. (b) Number of rotations = $\frac{72}{12} = 6$

$$=1\begin{bmatrix} \because \tan(90^\circ - \) = \cot \\ \cot(90^\circ - \) = \tan \\ \tan \ .\cot = 1 \end{bmatrix}$$
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38. (b)
$$a^2 + b^2 + c^2 = 2 (a - b - c) - 3$$

 $\Rightarrow a^2 + b^2 + c^2 - 2a + 2b + 2c + 3 = 0$
 $\Rightarrow a^2 -2a + 1 + b^2 + 2b + 1 + c^2 + 2c + 1=0$
 $\Rightarrow (a - 1)^2 + (b + 1)^2 + (c + 1)^2 = 0$
[If $x^2 + y^2 + z^2 = 0$
 $\Rightarrow x = 0; y = 0; z = 0$]
 $\therefore a - 1 = 0 \Rightarrow a = 1$
 $b + 1 = 0 \Rightarrow b = -1$
 $c + 1 = 0 \Rightarrow c = -1$
 $\therefore 2a - 3b + 4c = 2 + 3 - 4 = 1$
39. (c) 1st Part :

$$\frac{\frac{6+4+3}{12}}{\frac{1}{9}+\frac{1}{2}-\frac{1}{5}} = \frac{\frac{13}{12}}{\frac{2}{9}+\frac{2}{7}-\frac{2}{5}} = \frac{\frac{13}{12}}{\frac{34}{9\times7\times5}}$$

 $=\frac{13}{12} \times \left(\frac{9 \times 7 \times 5}{34}\right)$

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2nd Part : $\frac{28-2}{90} \times \frac{9}{100} \times \frac{35}{10}}{226-2} = \frac{26\times9\times35}{2204\times8\times1}$ ACHIEVERS In Focus $\frac{28-2}{90} \times \frac{9}{100} \times \frac{31}{10} = \frac{26\times9\times35}{204\times8\times1}$ $\therefore \quad \frac{13}{12} \times \frac{9\times7\times5}{34} \times \frac{204\times8\times1}{26\times9\times35} = 2$ 40. (d) $3.\overline{36} - 2.\overline{05} + 1.\overline{33}$ $= 3\frac{36}{99} - 2\frac{05}{99} + 1\frac{33}{99}$ $= 3 + \frac{36}{99} - 2 - \frac{5}{99} + 1 + \frac{33}{99}$ $= (3 - 2 + 1) + \left(\frac{36}{99} - \frac{5}{99} + \frac{33}{99}\right)$ $= 2 + \left(\frac{36-5+33}{99}\right) = 2 + \frac{64}{99} = 2\frac{64}{99} = 2.\overline{64}$ 41. (a) Required LCM $= \frac{\text{LCM of } 2.3.4.9}{\text{HCF of } 3.5.7.13}$ $= \frac{4\times9}{1} = 36$

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42.(a) Let original rate of rice be \gtrless x per kg.

Reduced rate =
$$\mathbf{R} \left[(100 - 6.25) \times \frac{1}{100} \times \mathbf{x} \right]$$

Achievers in Focus $= \mathbf{E} \frac{15x}{16}$ per kg

According to the question, $\frac{120}{15x} - \frac{120}{x} = 1$

 $\Rightarrow \frac{120}{x} \left(\frac{16}{15} - 1 \right) = 1$ $\therefore x = ₹ 8 \text{ per kg}$ $\therefore \text{ Reduced rate} = ₹ \left(\frac{15}{16} \times 8 \right) \text{ per kg}$

43. (d) Let the sum lent at the rate of interest 5% per annum is ₹ x. and at the rate of interest 8% per annum is ₹

(1550 - x)
According to the question,
$$\frac{x \times 5 \times 3}{100} + \frac{(1550 - x) \times 8 \times 3}{100} = 300$$
$$\Rightarrow \frac{15x}{100} + \frac{37200 - 24x}{100} = 300$$
$$\Rightarrow 15x + 37200 - 24x = 300 \times 100$$

$$\Rightarrow 9x = 7200 \quad \therefore x = ₹ 800$$

and, 1550 - x = 1550 - 800 = ₹ 750
$$\therefore \text{ Ratio of money lent at 5% to that at 8%} = 800 : 750 = 16 : 15$$

44. (b) If the C.P. of article be ₹ x.
then $x \times (105 - \frac{195}{2})\% = 12$
$$\Rightarrow x \times \frac{15}{200} = 12$$

$$\Rightarrow x \times \frac{15}{200} = 12$$

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$$\Rightarrow x = \frac{12 \times 200}{15} = ₹ 160$$

45. (a) A's 1 day's work = $\frac{1}{12}$
(A + B)'s 1 day's work = $\frac{1}{8}$
$$\therefore \text{ B's 1 day's work} = \frac{1}{8} - \frac{1}{12} = \frac{3-2}{24} = \frac{1}{24}$$

$$\therefore \text{ B alone can do the work in 24 days.}$$

46. (c) Let the mother's age
= x years
$$\therefore \text{ Father's age} = (x + 8) \text{ years}$$

Sum of ages of 6 sons
= 8 × 6 = 48 years
Sum of ages of 6 sons and parents
= 22 × 8 = 176 years.
$$\therefore \text{ Age of Parents} = 176 - 48 = 128 \text{ years}$$

$$\Rightarrow x + x + 8 = 128$$

$$\Rightarrow 2x = 120 \Rightarrow x = 60$$

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Hence, mother's age = 60 years
47. (d) Count the number of odd days from the year 2007
onwards to get the sum equal to 0 odd day.

 Year2007
 2008
 2009
 2010
 2011
 2012
 2013
 2014
 2015
 2016
 2017

 odd
 1
 2
 1
 1
 2
 1
 1
 2
 1

day

Sum = 14 odd days \equiv 0 odd day

Calendar for the year 2018 will be the same as for the year 2007.



 $\therefore \angle ABC = 180^\circ - 120^\circ = 60^\circ$

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 $\angle ACE = 105^{\circ}$ $\Rightarrow 2 = x + \frac{13}{17} \Rightarrow x = 2 - \frac{13}{17}$ ACHIEVERS In Focus $\therefore \angle ACB = 180^{\circ} - 105^{\circ} = 75^{\circ}$ $=\frac{34-13}{17}=\frac{21}{17}$ $\therefore \angle BAC = 180^{\circ} - 60^{\circ} - 75^{\circ} = 45^{\circ}$ **ACHIEVERS** In Focus Length of wire 49. (b) 52. (b) Let two numbers of 3 digits be 310x and 310y $=\frac{22}{7} \times 42 = 132$ cm. $\therefore 310x \times 310y = 310 \times 1860 \implies x \times y = 6$ Let the length of rectangle \therefore x = 2 and y = 3 i.e., 620 and 930 = 6x and breadth = 5x cm 53. (c) Given that a = 6% $\therefore 2 (6x + 5x) = 132$ $\Rightarrow 22x = 132 \quad \Rightarrow x = \frac{132}{22} = 6$ $\therefore \text{ Length of rectangle} = 36 \text{ cm and breadth} = 30 \text{ cm}$ According to the formula, Increase in consumption $=\left(\frac{a}{100-a}\times100\right)\%$ \therefore Area of rectangle = $36 \times 30 = 1080 \text{ cm}^2$ $\frac{a^{-1}}{a^{-1}+b^{-1}}+\frac{a^{-1}}{a^{-1}-b^{-1}}$ 50. (b) $= \left(\frac{6}{94} \times 100\right)\% = \frac{600}{94}\% = 6\frac{18}{47}\%$ $=\frac{\displaystyle\frac{1}{a}}{\displaystyle\frac{1}{a}+\displaystyle\frac{1}{b}}+\frac{\displaystyle\frac{1}{a}}{\displaystyle\frac{1}{a}-\displaystyle\frac{1}{b}}=\frac{\displaystyle\frac{1}{a}}{\displaystyle\frac{b+a}{ab}}+\frac{\displaystyle\frac{1}{a}}{\displaystyle\frac{b-a}{ab}}$ 54. (d) Work done by (A + B) in 20 days = $\left(\frac{1}{30} \times 20\right) = \frac{2}{3};$ $=\frac{1}{a}\cdot\frac{ab}{b+a}+\frac{1}{a}\cdot\frac{ab}{b-a}$ Remaining work $=\left(1-\frac{2}{3}\right) = \frac{1}{3}$ ACHIEVERS In Focus $=\frac{b}{b+a}+\frac{b}{b-a}$ $=\frac{b(b-a)+b(b+a)}{(b+a)(b-a)} = \frac{b^2-ab+b^2+ab}{b^2-a^2} = \frac{2b^2}{b^2-a^2}$ $\frac{1}{3}$ work is done by A in 20 days. Whole work is done by A in (20×3) days = 60 days $2 = x + \frac{1}{1 + \frac{1}{3 + \frac{1}{4}}}$ 51. (b) 55. (a) One is x yrs, another (x + 20) yrs. \therefore (x + 20) - 5 = 5(x - 5) or, x = 10 $\Rightarrow 2 = x + \frac{1}{1 + \frac{1}{\frac{12 + 1}{4}}}$ $\Rightarrow 2 = x + \frac{1}{1 + \frac{4}{13}}$: 30, 10 96. (d) abcd / aabbccdd / aaabbbcccddd. **ACHIEVERS** In Focus $Q^- - R^- - S^+$ 99. (d) ACHIEVERS In Focus $\Rightarrow 2 = x + \frac{1}{\frac{13+4}{13}} \Rightarrow 2 = x + \frac{1}{\frac{17}{13}}$